

# Stochastic Coordination in CAS: Expressiveness & Predictability

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DISI  
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- 1 Context, Motivation & Goals
- 2 Research Threads
  - Uniform Primitives
  - Probabilistic Modular Embedding
  - Biochemical Coordination
- 3 Future Directions & Open Questions



# Outline

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# Stochastic Coordination in CAS: Why

- CAS are usually composed of a *multitude of heterogeneous, autonomous agents*, which **needs to interact** in order to achieve a system goal—typically beyond their individual capabilities
  - ⇒ **coordination** is a fundamental concern when *both analysing and modelling* CAS
- CAS often exhibit **stochastic behaviours**, stemming from *probabilistic* and *time-dependent* local (interaction) mechanisms
  - ⇒ **stochastic coordination** models and languages provide such mechanisms

## Expressiveness & Predictability

Understanding *expressiveness* of coordination languages and achieving *predictability* of stochastic coordination models is a fundamental step in the quest for designing well-engineered CAS.

# Stochastic Coordination in CAS: Issues

**Expressiveness** from both the computer science and computer engineering points of view:

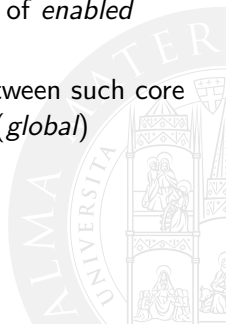
- science — formal expressiveness of *coordination languages* (to *observe* systems) [Bonsangue et al., 2003]
- engineering — *core coordination mechanisms* enabling expression of collective behaviours (to *build* systems) [Fernandez-Marquez et al., 2012b]

**Predictability** in terms of the “*local-to-global*” issue [Beal and Bachrach, 2006] of CAS

- design the *local* interaction mechanisms to achieve desired *global* behaviour
- ... (and the other way around: encode the global behaviour in terms of the local mechanisms available)

# Stochastic Coordination in CAS: Goals

- 1 Devise out **core coordination mechanisms** enabling *self-organisation and adaptiveness* in CAS
- 2 Understand their **expressiveness**, both in terms of *formal comparison* of languages' (relative) expressive power and in terms of *enabled "behaviours"*
- 3 Ensure **predictable** (and controllable) **relationships** between such core (*local*) mechanisms and the overall coordinated CAS (*global*) behaviour exist



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# Motivation & Goals

- LINDA [Gelernter, 1985] features *don't know* non-determinism handled with a *don't care* approach:
  - don't know* which tuple among the matching ones is retrieved by a getter operation (`in`, `rd`) can be neither specified nor predicted
  - don't care* nonetheless, the coordinated system (e.g. the CAS) is designed so as to keep on working whichever is the matching tuple returned

## LINDA & CAS

CAS may need to implement *stochastic behaviours* like “*most of the time do this, but sometimes do that*”.

# A Core Coordination Mechanism

- We define **uniform coordination primitives** (`uin`, `urd`) – first mentioned in [Gardelli et al., 2007] – as the specialisation of LINDA getter primitives featuring *probabilistic non-determinism* [Mariani and Omicini, 2014]

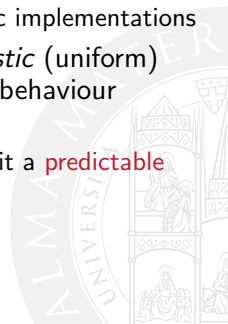
## The uLINDA Approach

Uniform primitives allow CAS designers to both specify and (*statistically*) **predict** the probability to retrieve one specific (kind of) tuple among a bag of matching tuples.

- Uniform primitives are (one of) the **core coordination mechanisms** enabling self-organisation in CAS: a *minimal construct* able (alone) to impact the *observable properties* of a coordinated system

# On Predictability I

- In a sequence of getter operations, **LINDA** *don't know* non-determinism makes any prediction of the overall behaviour impossible
  - sequences of LINDA getter operations present **no predictable distribution** over time—abstracting away from specific implementations
- In a sequence of getter operations, **ULINDA** *probabilistic* (uniform) non-determinism makes predictions about the overall behaviour possible
  - sequences of ULINDA getter operations tend to exhibit a **predictable uniform distribution** over time



# On Predictability II

## A Dice in LINDA

- We define tuple space dice
- We represent a six-face dice as a collection of six tuples: `face(1)`, ..., `face(6)`
- We roll a dice by **rd-ing** a face/1 tuple from dice: `dice ? rd(face(X))`
- ! We **do not** obtain the (stochastic) behaviour of a dice: e.g., it may *reasonably* happen that rolling the dice  $10^9$  times always results in X/1



# On Predictability III

## A Dice in uLINDA

- Again, we define tuple space dice
- Again, we represent a six-face dice as a collection of six tuples:  
`face(1), ..., face(6)`
- We roll a dice by **urd-ing** a `face/1` tuple from dice: `dice ? urd(face(X))`
- ! Now, we **do** obtain the (stochastic) behaviour of a dice: repeating several times a roll, the six faces will tend to converge towards a uniform distribution



# On Expressiveness: “Load Balancing” I

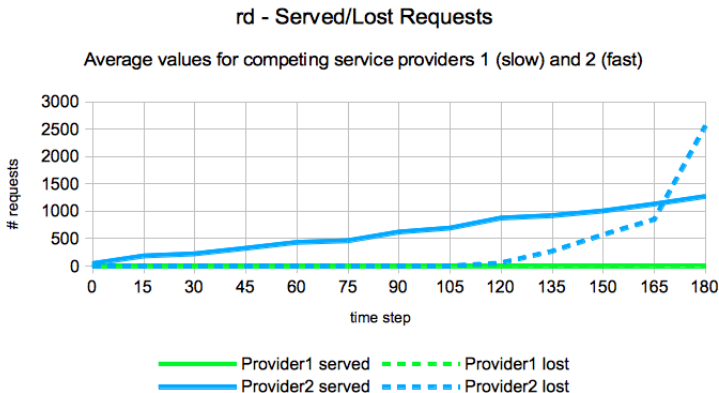


Figure : Clients using rd: Provider1 is under-exploited—actually, not at all. Notice it could be Provider2, **we don't know “a priori”**.

# On Expressiveness: “Load Balancing” II

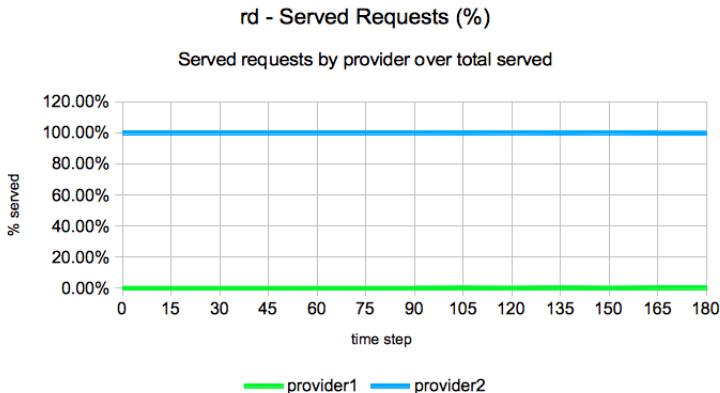


Figure : Provider1 and Provider2 exhibit no collective behaviour—no “load balancing”.

# On Expressiveness: “Load Balancing” III

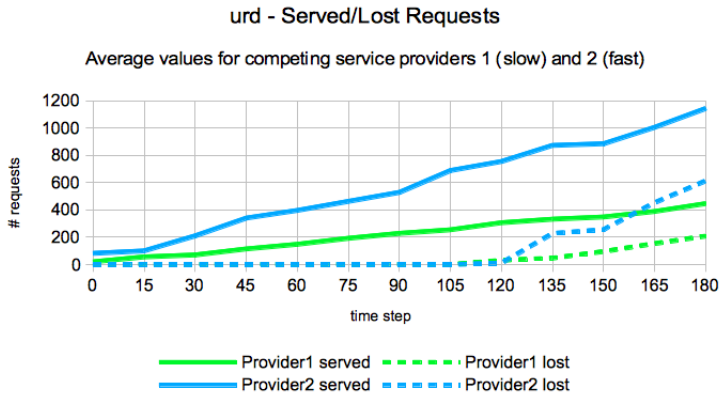


Figure : Clients using urd: Provider2 is exploited as much as it can afford. Provider1 takes what's left.



# On Expressiveness: “Load Balancing” IV

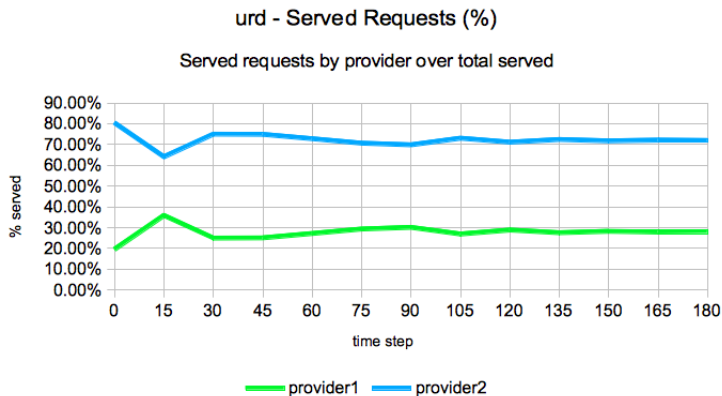


Figure : Provider1 and Provider2 exhibit some form of “load balancing”, achieved by self-organisation.

# On Expressiveness: “Stigmergic Coordination” I

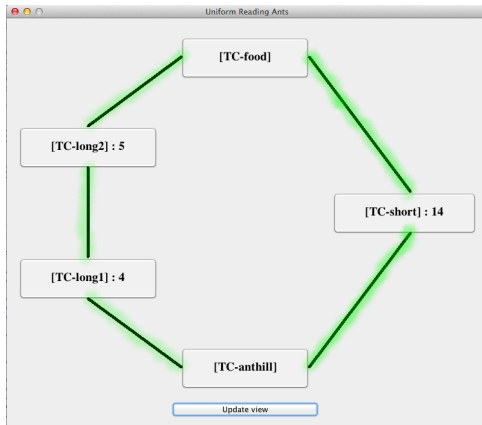


Figure : Digital ants search for food (top box) wandering **randomly** from their anthill (bottom box).

# On Expressiveness: “Stigmergic Coordination” II

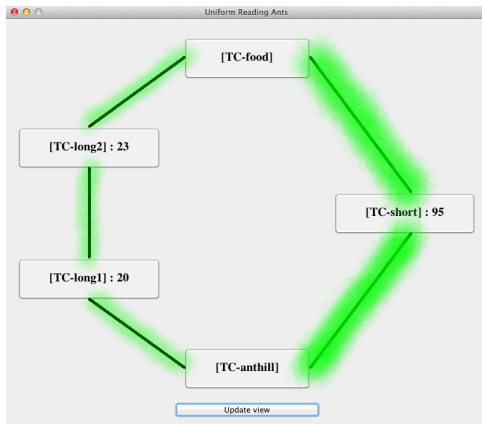


Figure : By understanding digital pheromones, ants find the optimal path toward the food source—as a self-organising, distributed process.

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# Motivation & Goals

- Understanding **expressiveness** of coordination languages is essential to deal with *interactions complexity* [Wegner, 1997]
- The notion of *Modular Embedding* [de Boer and Palamidessi, 1994] has been proposed for comparison of the **relative expressiveness** of *concurrent languages*

## Expressiveness & CAS

CAS features **stochastic** behaviours, exploiting *probabilistic mechanisms*, which demands new techniques to model and *measure expressiveness*.

# A New Measure of Expressiveness I

## (Modular) Embedding

The informal definition of (modular) *embedding* assumes that a language could be translated in another [Shapiro, 1991]

**easily** “without the need for a global reorganisation of the program”

**equivalently** “without affecting the program’s observable behaviour”

- We refine term “easily” to focus on **coordination languages’ expressiveness**:
  - no *extra-computations* to mimic complex coordination operators
  - no *extra-coordinators* (neither coordinated processes nor coordination medium) to avoid suspensive semantics
  - no *unbound extra-interactions* to perform additional coordination

# A New Measure of Expressiveness II

- We refine term “equivalently” to cover **probabilistic coordination languages**:
  - observable actions should be associated with their *execution probability*, driven by synchronisation opportunities offered by the coordination medium at run-time
  - ending states should be defined as those states for which all outgoing transitions have probability 0. Also, they should be refined with the probability of reaching that state from a given initial one

## Probabilistic Modular Embedding

Using these refined definitions of “easily” and “equivalently”<sup>a</sup>, we shift from Modular Embedding to **Probabilistic Modular Embedding** [Mariani and Omicini, 2013].

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<sup>a</sup>It's a long story short, for the precise formalisation see the cited paper.

# On Expressiveness I

- Suppose a ProbLinCa<sup>1</sup> process  $P$  and a LinCa process  $Q$  are acting on tuple space  $S$ :

$$P = \text{in}_p(T).\emptyset + \text{in}_p(T).\text{rd}_p(T').\emptyset$$

$$Q = \text{in}(T).\emptyset + \text{in}(T).\text{rd}(T').\emptyset$$

$$S = \langle \mathbf{t}_1[20], \mathbf{t}_r[10] \rangle$$

where  $T$  is a LINDA template matching both tuples  $\mathbf{t}_1$  and  $\mathbf{t}_r$ , whereas  $T'$  matches  $\mathbf{t}_r$  solely.

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<sup>1</sup>Probabilistic extension of the LINDA-based LinCa calculus, in which each tuple has a *weight* resembling **selection probability**: the higher the weight, the higher the matching chance [Bravetti et al., 2005].



# On Expressiveness II

## Modular Embedding

To ME,  $P$  and  $Q$  are *not distinguishable*, being their ending states the same:

$$\Psi[P] = (\text{success}, \langle t_r[10] \rangle) \text{ OR } (\text{deadlock}, \langle t_l[20] \rangle)$$

$$\Psi[Q] = (\text{success}, \langle t_r[10] \rangle) \text{ OR } (\text{deadlock}, \langle t_l[20] \rangle)$$

## Quantity vs. Quality

Whereas  $P$  and  $Q$  are **qualitatively** equivalent, they are not so **quantitatively**, but ME cannot tell apart the probabilistic information conveyed by, e.g., a ProbLinCa primitive w.r.t. a LinCa one<sup>a</sup>.

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<sup>a</sup>Similar results can be obtained comparing pKLAIM to KLAIM and  $\pi_{pa}$ -calculus (probabilistic asynchronous pi-calculus) to  $\pi_a$ -calculus (asynchronous pi-calculus) [Mariani and Omicini, 2013].

# On Expressiveness III

## Probabilistic Modular Embedding

By repeating the embedding observation, now using PME, we get:

$$\Phi[P] = (0.\bar{6}, \text{success}) \text{ OR } (0.\bar{3}, \text{deadlock})$$

$$\Phi[Q] = (\bullet, \text{success}) \text{ OR } (\bullet, \text{deadlock})$$

where symbol  $\bullet$  denotes “absence of information”.

## Quantity vs. Quality

PME succeeds in telling ProbLinCa apart from LinCa, recognising ProbLinCa as *more expressive* than LinCa, because it takes into account the probabilistic (**quantitative**) information conveyed by, e.g., a ProbLinCa primitive w.r.t. a LinCa one.

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# Motivation & Goals I

- Existing approaches to alleviate the so-called “local-to-global” issue [Beal and Bachrach, 2006] in CAS are mostly based on:
  - simulation [Gardelli et al., 2006]
  - parameter tuning [Gardelli et al., 2009]
  - (approximate) model checking [Casadei and Viroli, 2013]
  - “bio-inspired design patterns” [Fernandez-Marquez et al., 2012a]

## Limits

- simulation may not be able to accurately reproduce real world contingencies
- parameter tuning may lead to sub-optimal settings
- model checking may be impractical for the complexity of the problem at hand
- design patterns give no guarantees about the quality of the solution

# Motivation & Goals II

## Goals

We propose an integrated approach [Mariani, 2014]:

- 1 rely on *design patterns* — design the **local mechanisms** by implementing self-organisation primitives as **artificial chemical reactions**
- 2 go beyond the *law of mass action* [Cardelli, 2008] — engineer **custom kinetic rates** for such reactions
- 3 “simulate-then-tune” [Gardelli et al., 2008] — adjust the dynamics of the (artificial) chemical system obtained (the CAS) to achieve the emergent, global behaviour desired

# On Expressiveness I

- A survey of state-of-art literature<sup>2</sup> led to the following *core set of primitives*—the **local mechanisms**:

**decay** destroys information as time passes

**feed** increases information “relevance” (e.g. quantity)  
according to some kind of feedback mechanism

**activation/inhibition** changes information “status” (e.g. attributes, values, etc.) depending on external stimuli

**aggregation** fuses information together (e.g. filtering, merging, composing, transforming, etc.)

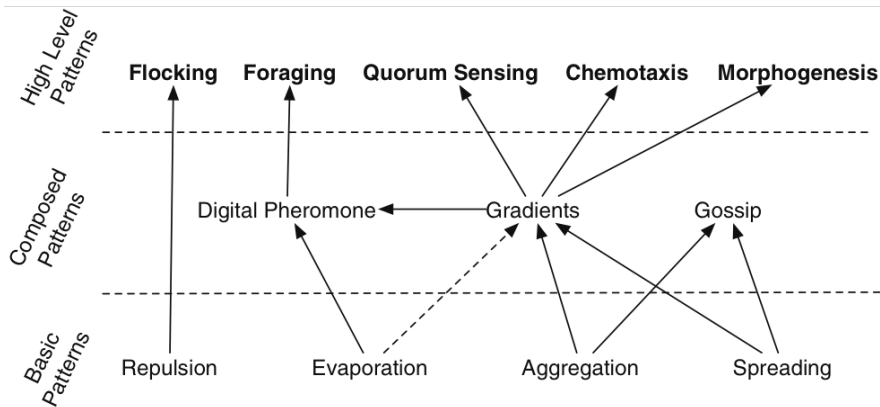
**diffusion** moves information within a topology (e.g. migration, replication, etc.)

**repulsion/attraction** drifts apart / approaches information

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<sup>2</sup>[Nagpal, 2004], [De Wolf and Holvoet, 2007], [Fernandez-Marquez et al., 2012b], [Fernandez-Marquez et al., 2011], [Tchao et al., 2011], [Viroli et al., 2011]

# On Expressiveness II



**Figure :** Bio-inspired design patterns, from *primitives* (local mechanisms) to high-level *patterns* (global behaviours). Image taken from [Fernandez-Marquez et al., 2012a].

# On Predictability I

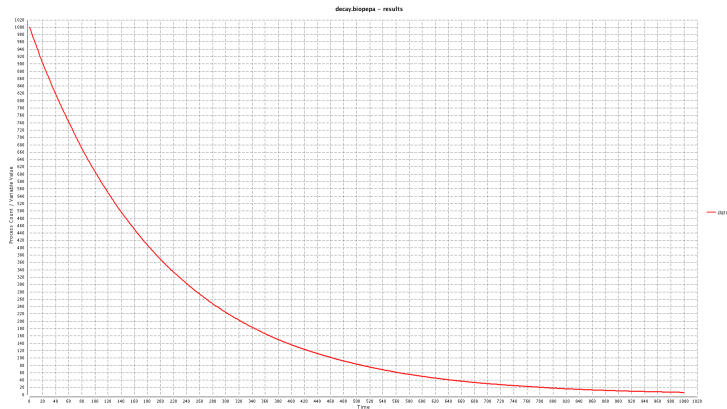
## From Local to Global

By engineering the *local mechanisms* as artificial *chemical reactions*, and by engineering *custom kinetic rates*, we can **relate** changes in local mechanisms to the global behaviour of the CAS and **observe/modify** such relationships.



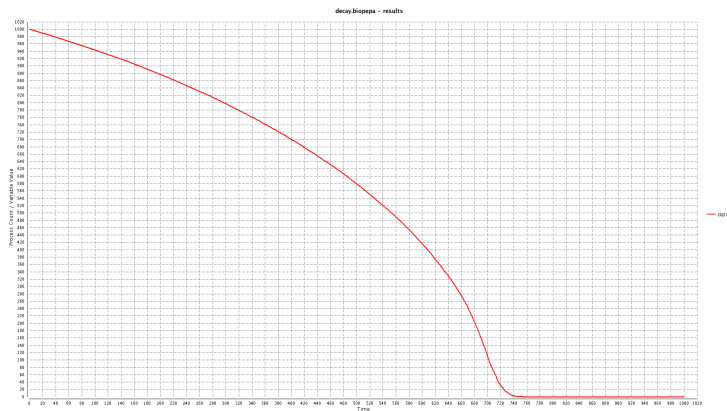


# On Predictability II



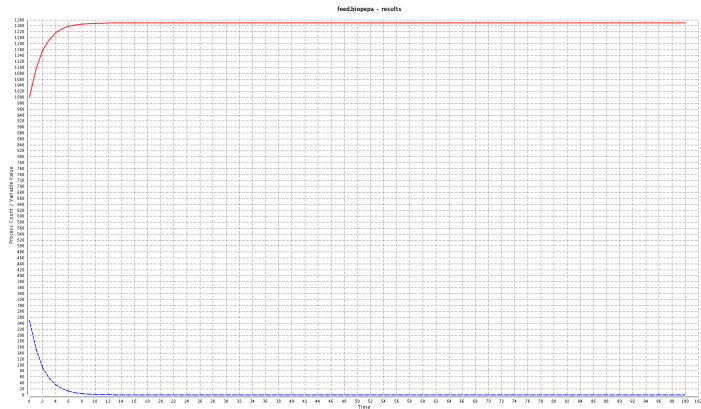
**Figure :** Decay chemical reaction, “fast-then-slow” trend, independent of the quantity of molecule to decay.

# On Predictability III



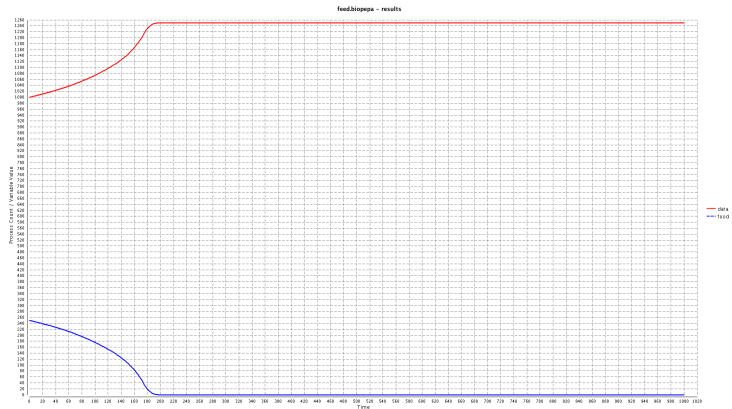
**Figure :** Decay chemical reaction, “slow-then-fast” trend, now dependent on the quantity of molecule to decay.

# On Predictability IV



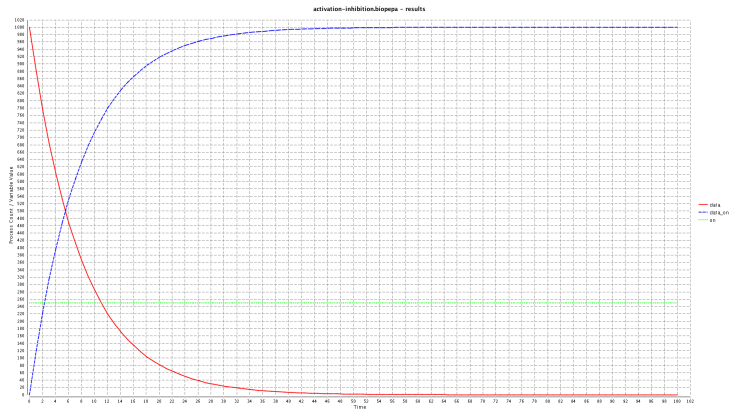
**Figure :** Feed chemical reaction, “fast-then-slow” trend, independent of the quantity of molecule to feed.

# On Predictability V



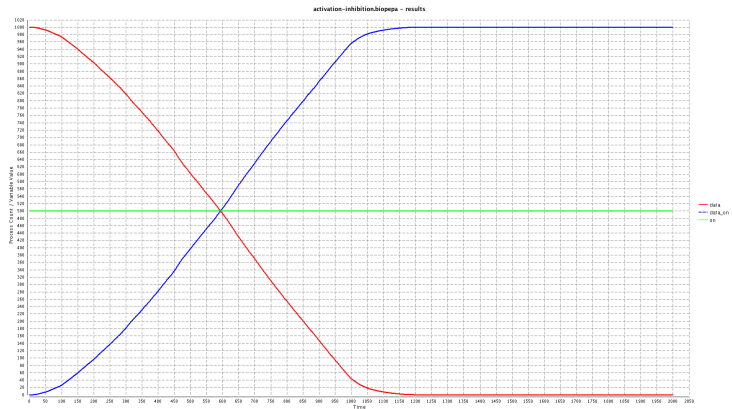
**Figure :** Feed chemical reaction, “slow-then-fast” trend, still independent of the quantity of molecule to feed.

# On Predictability VI



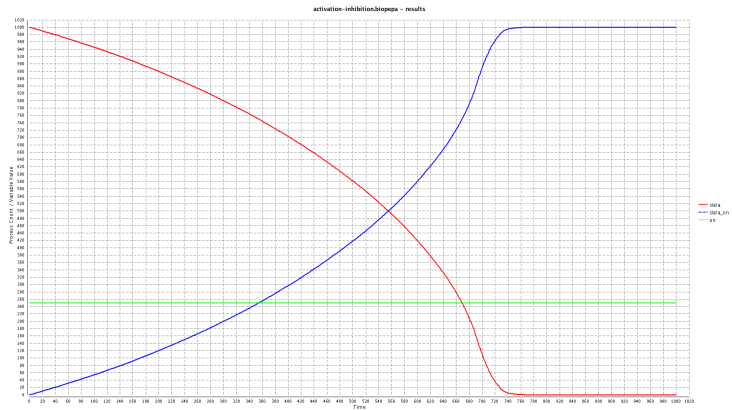
**Figure :** Activation chemical reaction, “fast-then-slow” trend, dependent on the quantity of activating molecule, independent of the quantity of molecule to activate.

# On Predictability VII



**Figure :** Activation chemical reaction, “nearly linear” trend, now independent of the quantity of activating molecule, now directly proportional to the quantity of molecule to activate.

# On Predictability VIII



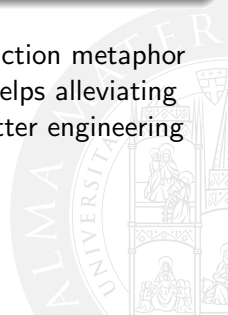
**Figure :** Activation chemical reaction, “slow-then-fast” trend, still independent of the quantity of activating molecule, still directly proportional to the quantity of molecule to activate.

# On Predictability IX

## Predictability

The factors chosen for custom kinetic rate expressions (the *local* mechanisms) have a well-defined, **predictable** effect on the *global* behaviour achieved by the CAS.

- This is made possible by adoption of the chemical reaction metaphor while implementing self-organisation primitives, and helps alleviating the “local-to-global” issue, ultimately leading to a better engineering of CAS behaviours





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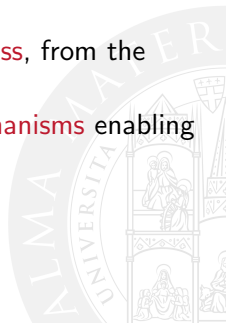
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# Future Directions I

**Uniform Primitives** Devising out *the whole spectrum* of self-organising behaviours they *directly enable* is essential to

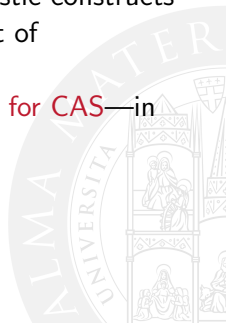
- understand their **modelling** capabilities, from the perspective of a CAS designer
- understand their (practical) **expressiveness**, from the perspective of a CAS developer
- build a **library of core coordination mechanisms** enabling and supporting self-organisation in CAS



## Future Directions II

**PME** Extending and further evaluating PME to *as many languages* as possible is essential to

- tell apart probabilistic languages into hierarchies of embeddings, devising out the **core** linguistic constructs from the “syntactic sugar”—in the spirit of [Vanglabbeek et al., 1995]
- define a novel notion of **Turing Machine for CAS**—in the spirit of [Wegner and Goldin, 2003]



# Future Directions III

**Biochemical Coordination** Investigating effectiveness of artificial chemical reactions in *modelling bio-inspired design patterns* is essential to

- devise out **expressiveness** of the biochemical metaphor applied to coordination in CAS
- improve **predictability** of the *global* behaviours exhibited by the CAS



# Open Questions

- ? How to know that a given set of *core* coordination mechanisms is **complete**? E.g. in the sense that it enables the *whole* spectrum of CAS self-organising behaviours?
- ? From the point of view of CAS engineering, what is the consequence of having different probability models placed in a *hierarchy* of embeddings? Does this imply a difference (even a hierarchy?) in the global behaviours they enable?
- ? Can we do what Wegner did with *Persistent Turing Machines* [Goldin, 2000], w.r.t. the interaction space of computations, in the field of CAS, building a theory of a **Collective Adaptive Turing Machine**?
- ? Is the biochemical metaphor scalable enough for large-scale CAS, e.g. world-wide socio-technical systems?

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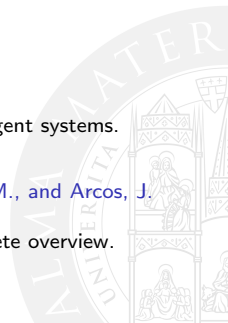
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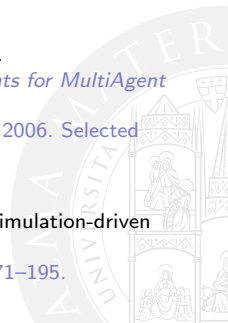
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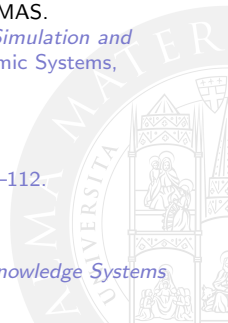
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# Stochastic Coordination in CAS: Expressiveness & Predictability

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